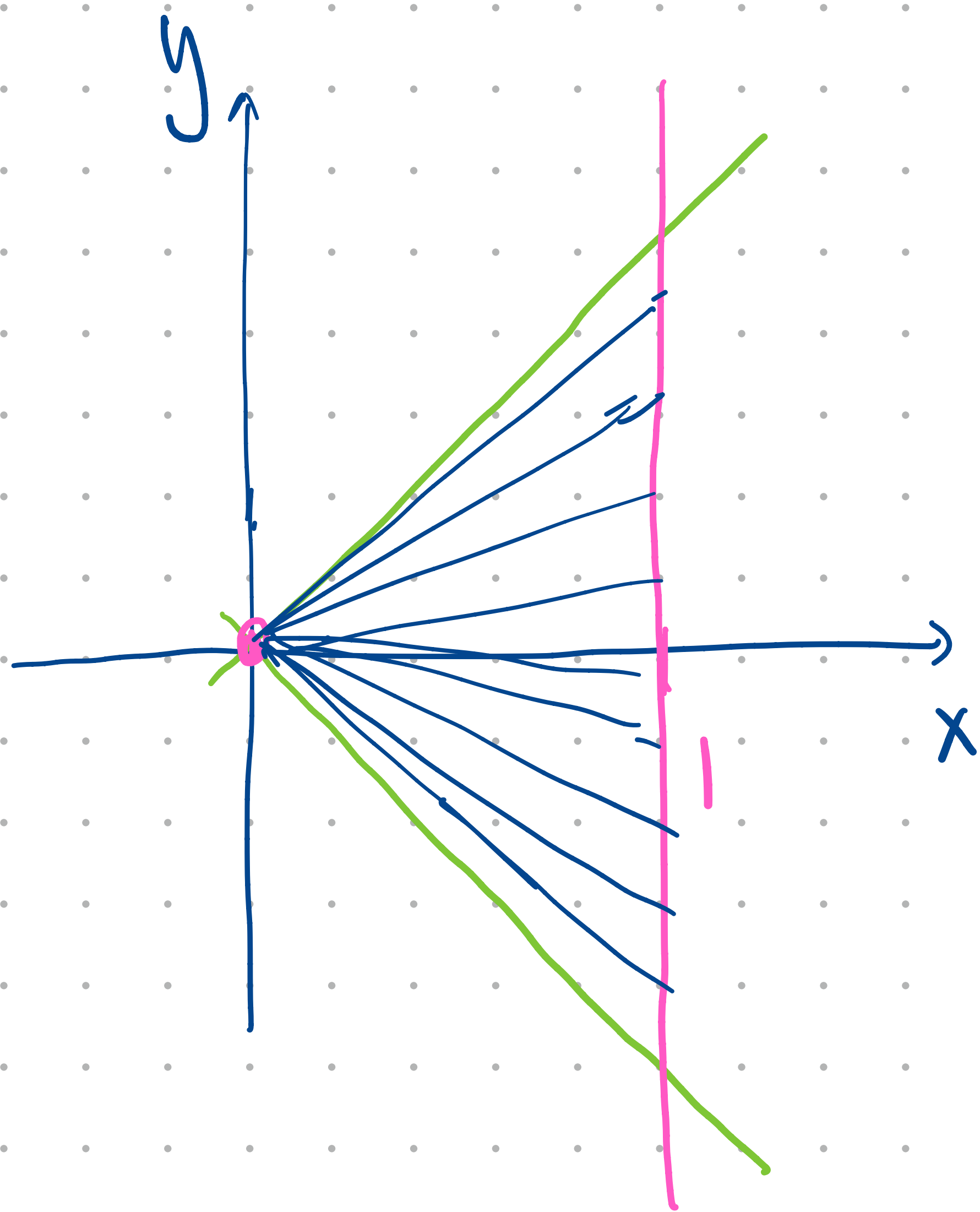


Compute the below by converting to Cartesian

$$\int_{-\pi/4}^{\pi/4} \int_0^{\sec \theta} r^4 \cos \theta \, dr \, d\theta$$



$$x = r \cos \theta$$

$$y = r \sin \theta$$

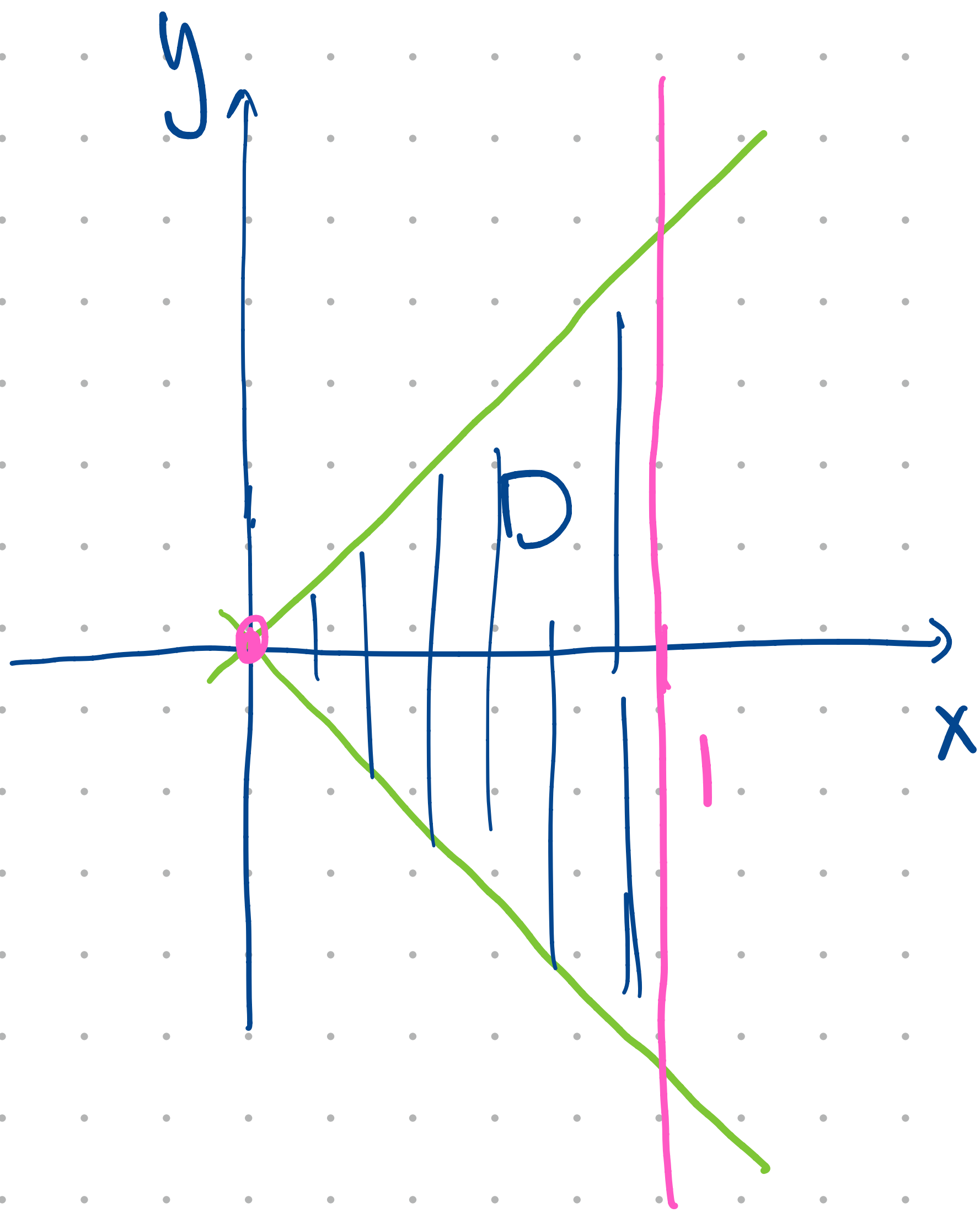
$$-\frac{\pi}{4} \leq \theta \leq \frac{\pi}{4}$$

$$0 \leq r \leq \sec \theta$$

$$r = \sec \theta$$

$$r \cos \theta = 1$$

$$x = 1$$



$$r^4 \cos \theta \, dr \, d\theta$$

$$= r^3 \cos \theta \underbrace{r \, dr \, d\theta}_{\substack{dx \, dy \\ \text{or } dy \, dx}}$$

$$= (r^2) (r \cos \theta) \, dx \, dy$$

$$= (x^2 + y^2) x \, dx \, dy$$

$$\iint_D (x^3 + xy^2) \, dx \, dy$$

or

$$dy \, dx \leftarrow$$

this only needs
one integral

$$= \int_0^1 \int_{-x}^x (x^3 + xy^2) \, dy \, dx = \dots$$

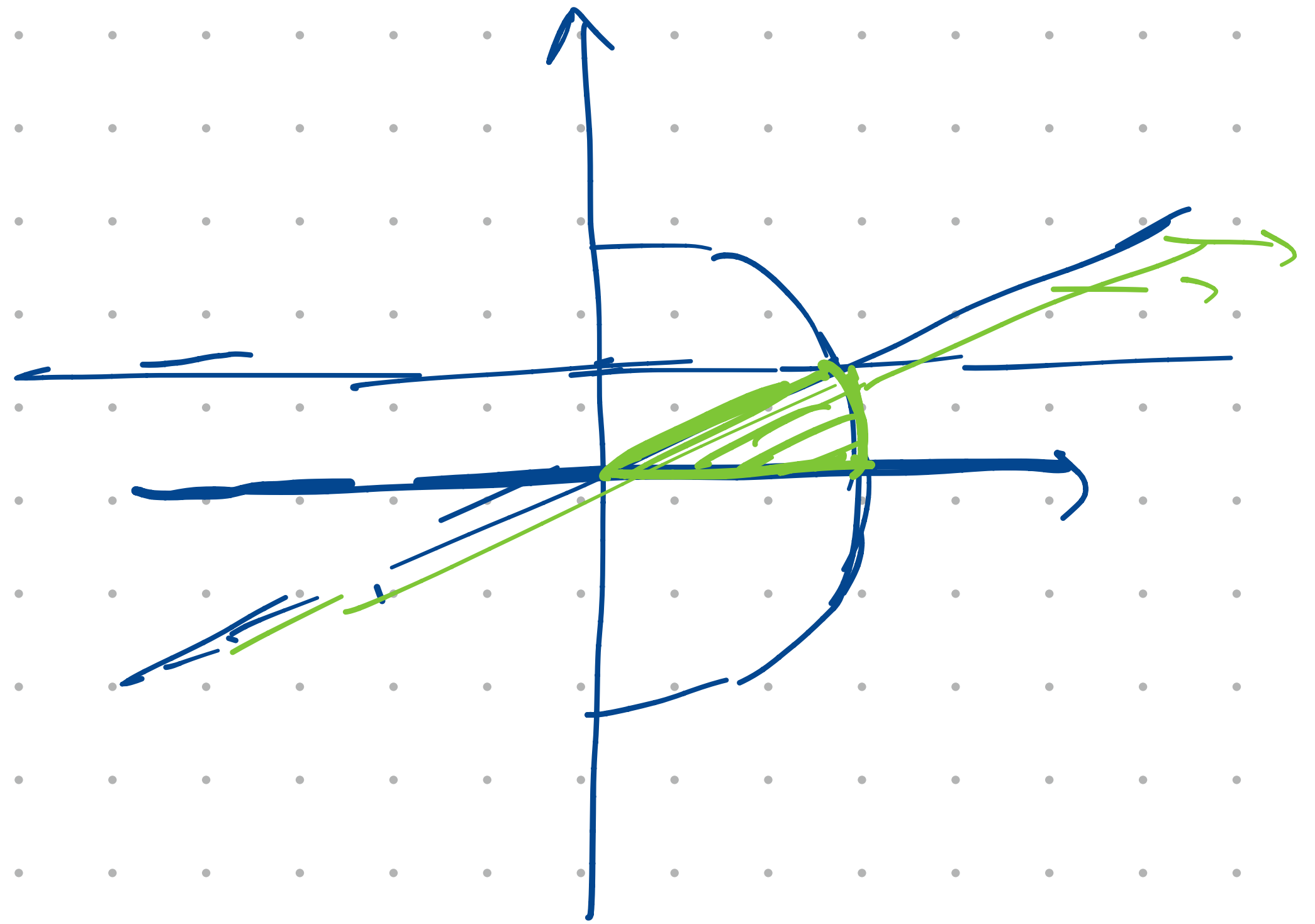
$$= \frac{8}{15}$$

#15.3.31

$$\int_0^{1/2} \int_{\sqrt{3}y}^{\sqrt{1-y^2}} dx dy$$

$$\sqrt{3}y \leq x \leq \sqrt{1-y^2}$$

$$0 \leq y \leq 1/2$$



- $\sqrt{3}y = x$

- $x = \sqrt{1-y^2}$

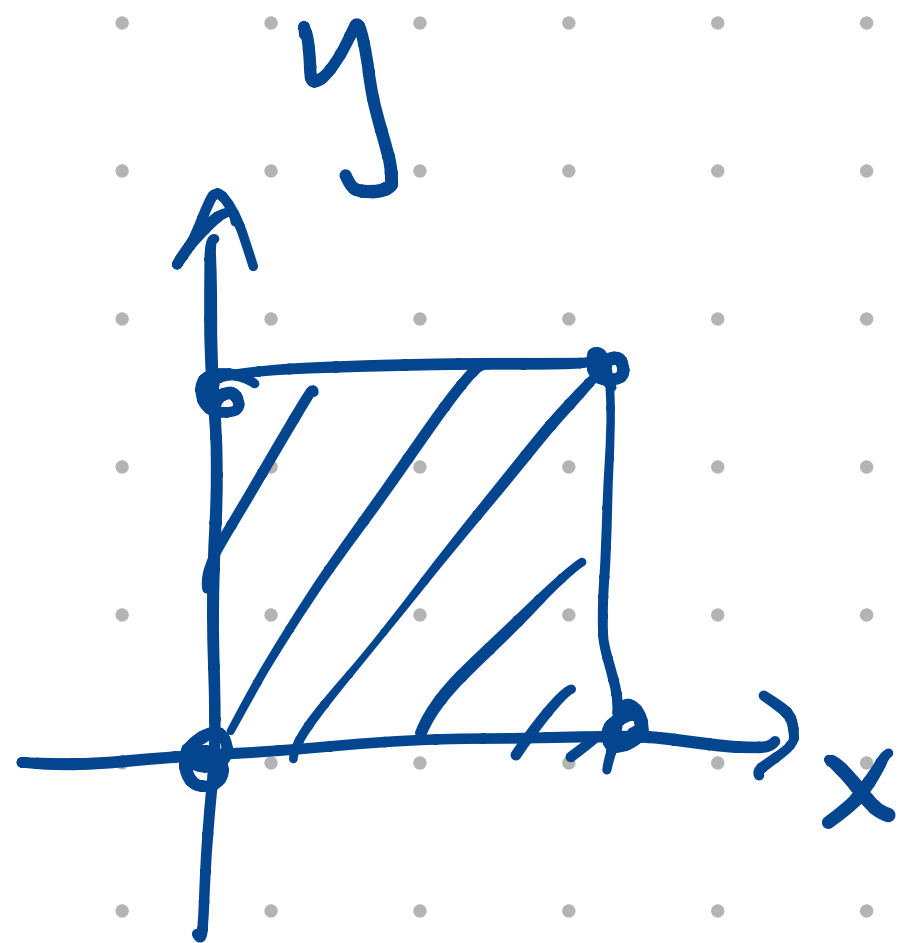
$$x^2 = 1 - y^2, \quad x^2 + y^2 = 1$$

- $y = 0$

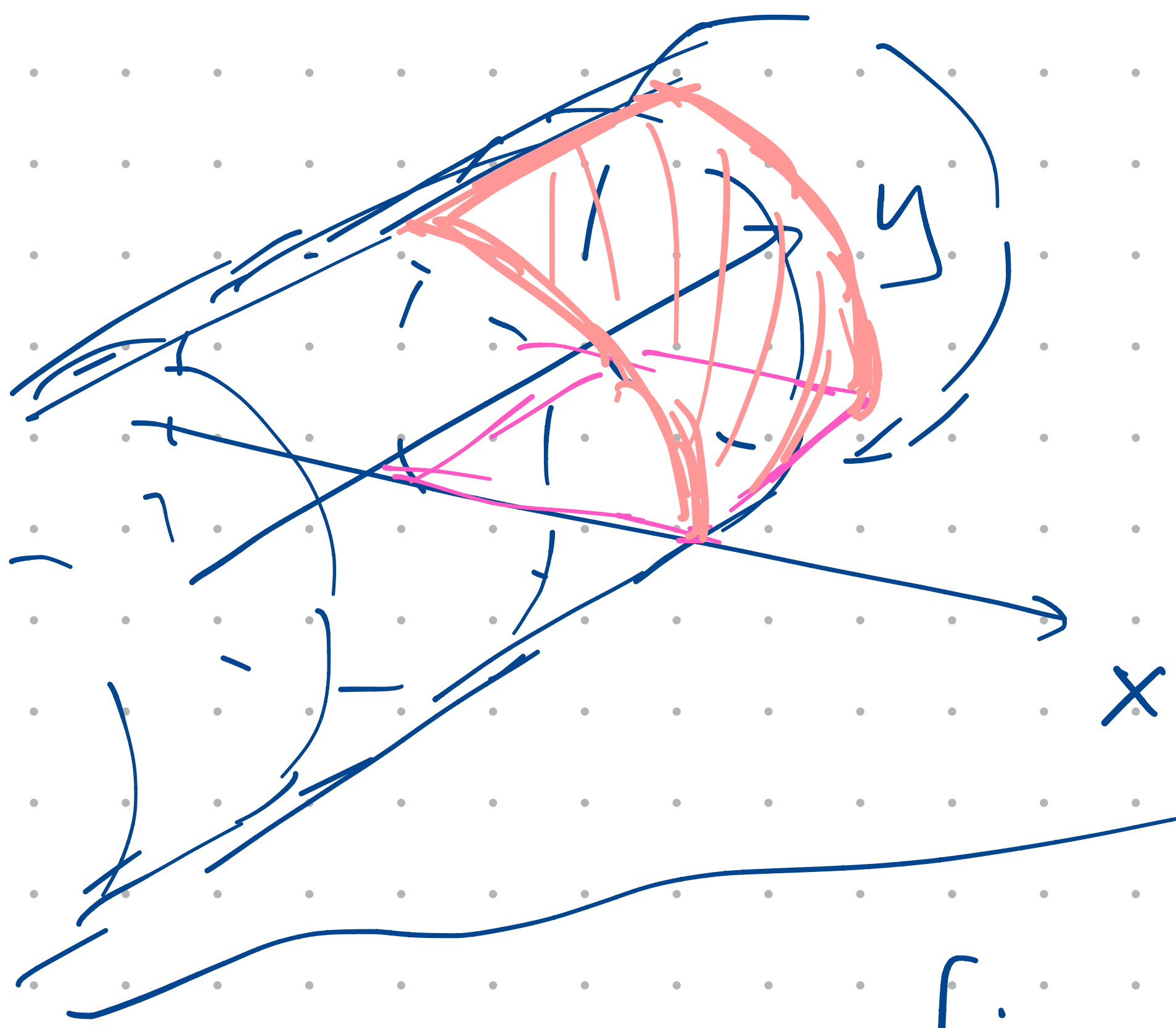
- $y = 1/2$

#15.5.6

part of $x^2 + z^2 = 4$ above



$$z = +\sqrt{4 - x^2} = f(x, y)$$



$$\int_0^1 \int_0^1 \sqrt{f_x^2 + f_y^2 + 1} \, dx \, dy$$

then compute...

Language comment:

The part of inside of

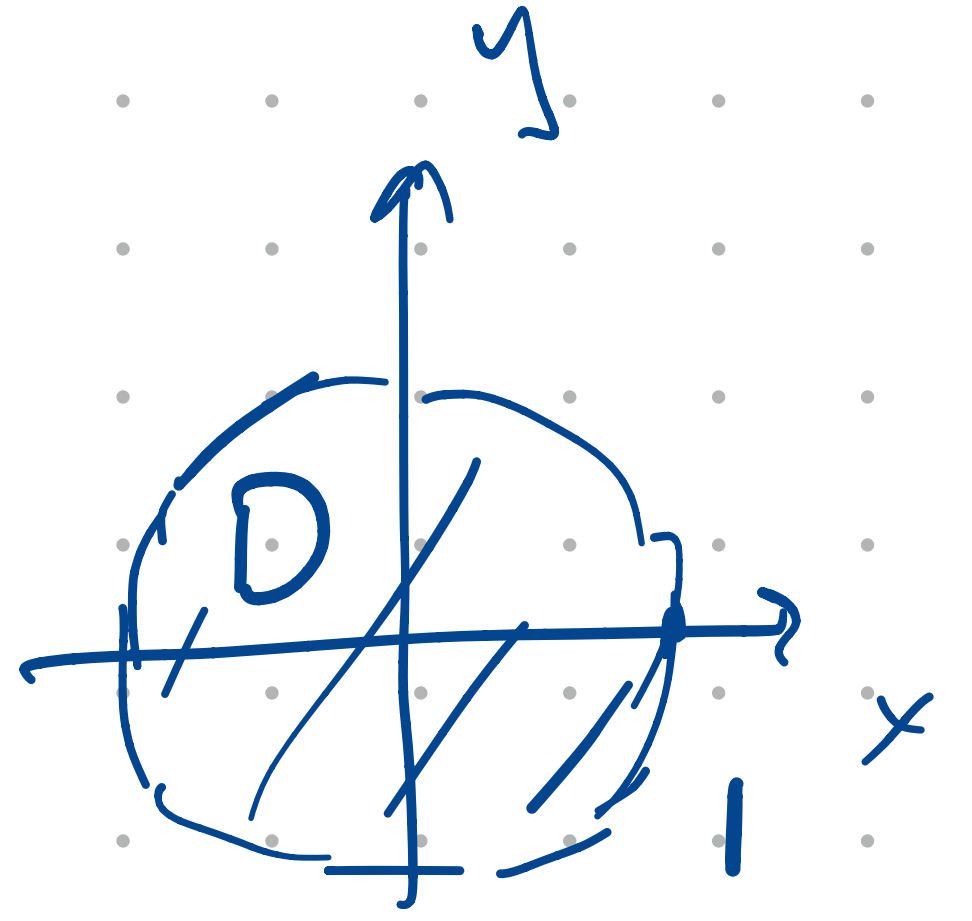
↑
determines the
integrand

↑
determine
the bounds.

#15.5.13 $f(x,y)$

$$z = \frac{1}{1+x^2+y^2}$$

over



$$\iint_D \sqrt{f_x^2 + f_y^2 + 1} \, dx \, dy$$

$$f_x(x,y) = -(1+x^2+y^2)^{-2} (2x)$$

$$(f_x(x,y))^2 = \frac{4x^2}{(1+x^2+y^2)^4}$$

$$\iint_D \sqrt{\frac{4x^2 + 4y^2}{(1+x^2+y^2)^4} + 1} \, dx \, dy$$

$$= \int_0^{2\pi} \int_0^1 \sqrt{\frac{4r^2}{(1+r^2)^4} + 1} \cdot r \, dr \, d\theta$$

$$= \int_0^1 \sqrt{\frac{4r^2}{(1+r^2)^4} + 1} \cdot r \, dr \cdot 2\pi$$

... in 1D

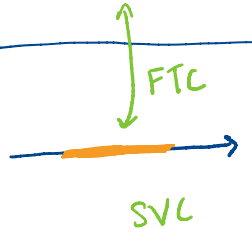
... in 2D

... in 3D

0D region ...

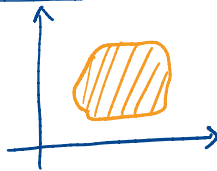


1D regions ...



2D regions ...

N/A



3D regions ...

N/A

N/A

